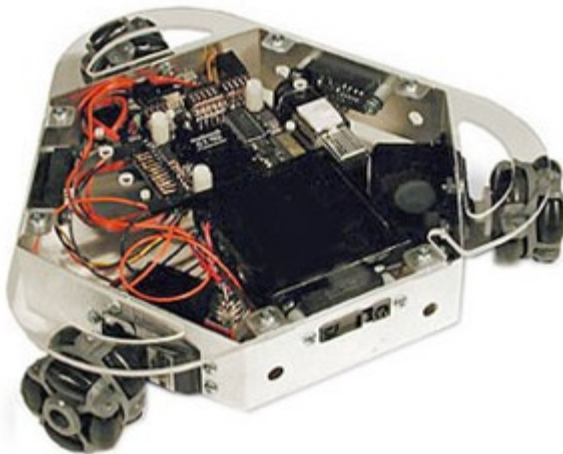
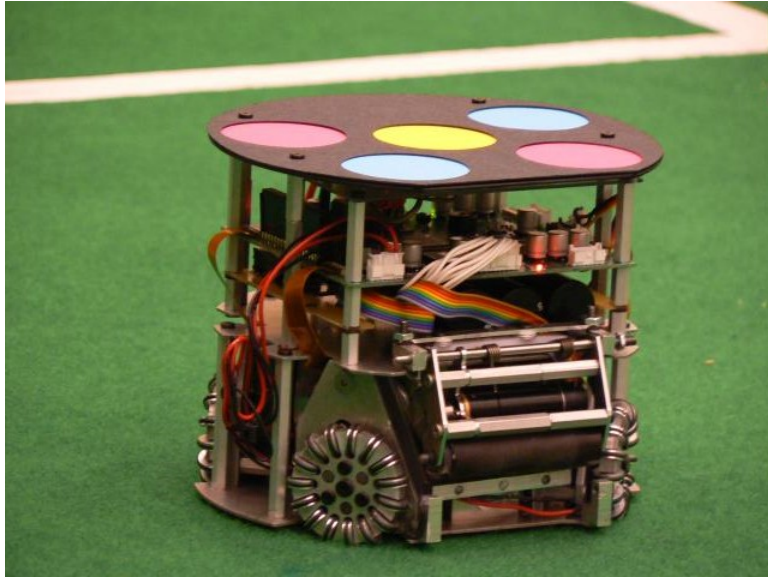


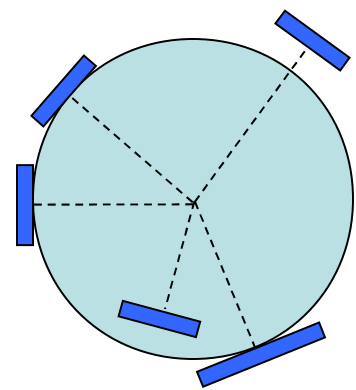
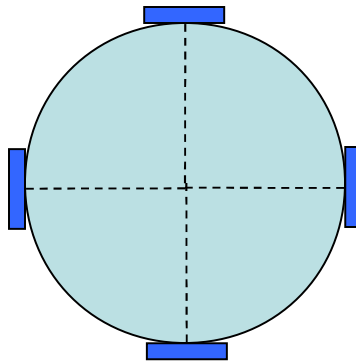
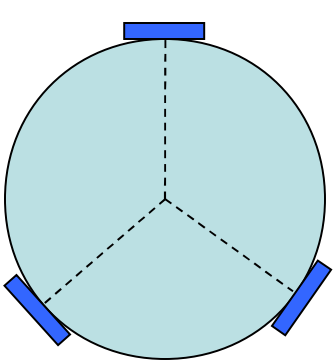
# Holonomic Robots



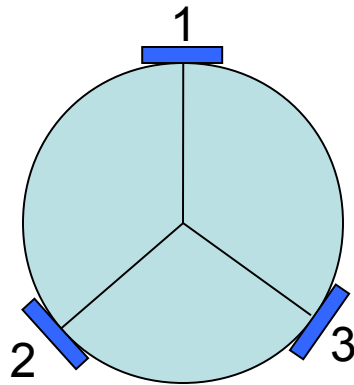
Ben Axelrod

Dec. 2009

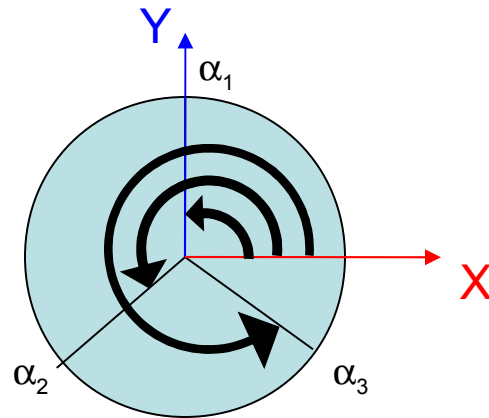




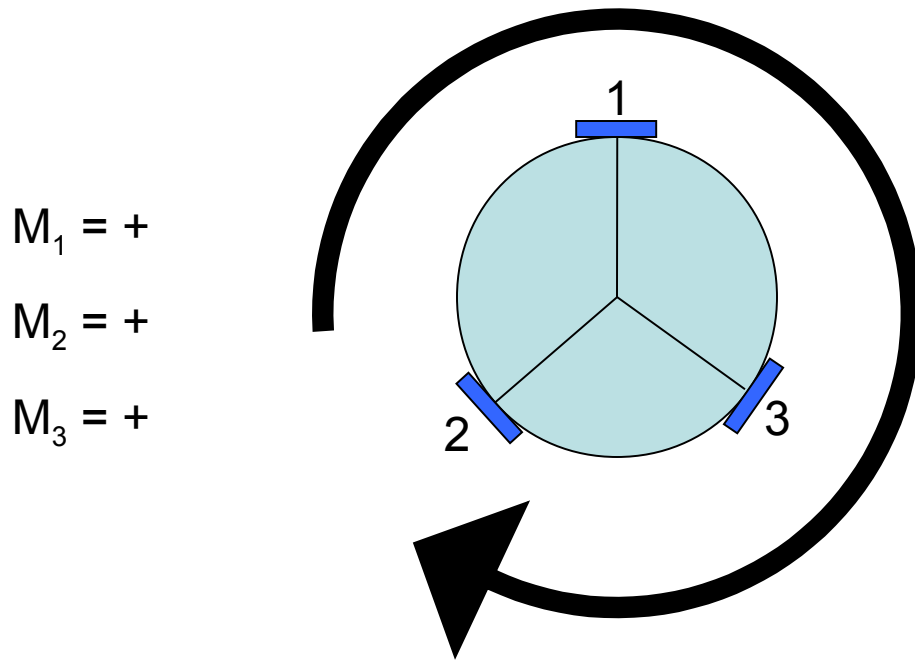
- Variable number of wheels, radius, and wheel sizes are possible



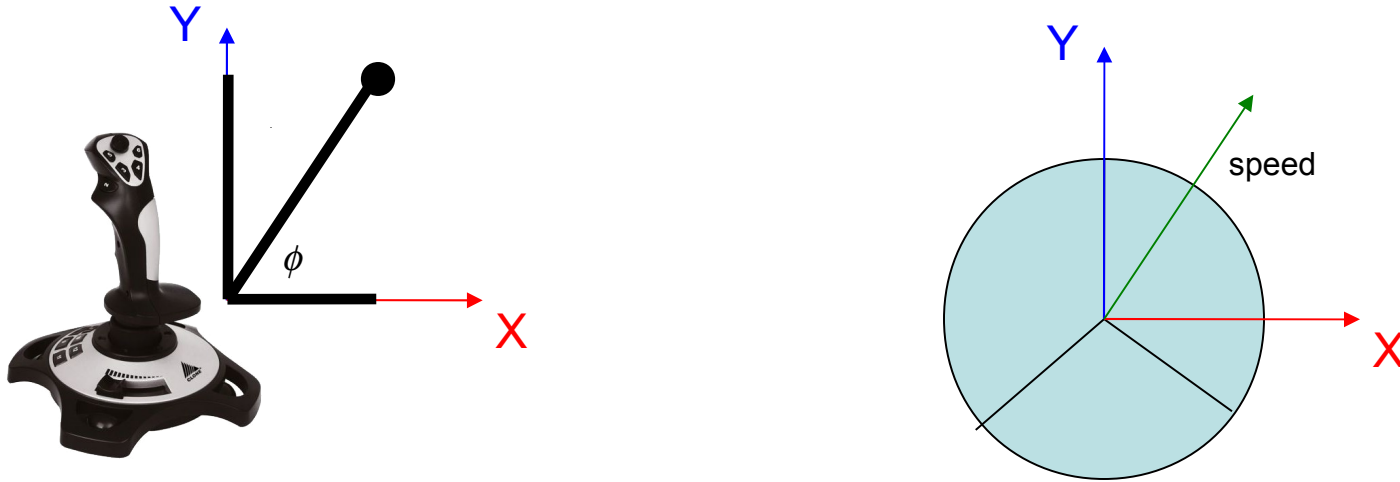
- We will examine a 3 wheel robot



- Create a coordinate system
- Record angle to each wheel:  $\alpha_1$   $\alpha_2$   $\alpha_3$



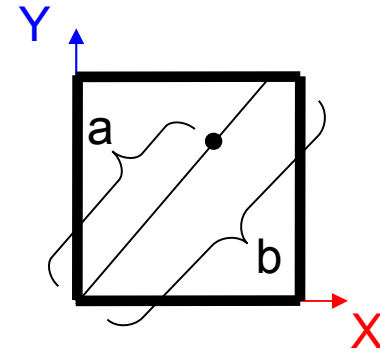
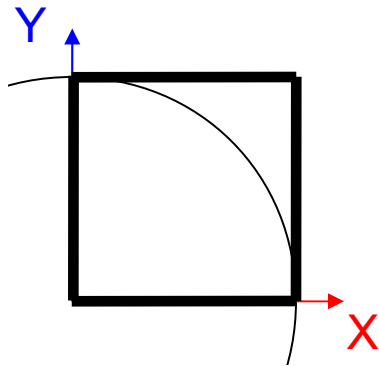
- Positive values sent to wheels spin robot clockwise



- Direction vector from joystick
- Angle  $\phi = \text{atan2}( Y \text{ joystick } , X \text{ joystick } )$ ;
- Scale vector such that length = speed

# Warning:

$$\sqrt{Y_{\max}^2 + X_{\max}^2} > Y_{\max}$$

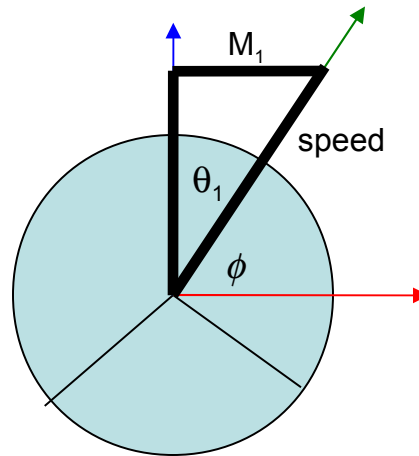


$$a = \sqrt{Y_{\text{joystick}}^2 + X_{\text{joystick}}^2}$$

$$\text{speed} = \text{maxspeed} \cdot \frac{a}{b}$$



# Wheel 1



$$\theta_1 = \alpha_1 - \phi$$

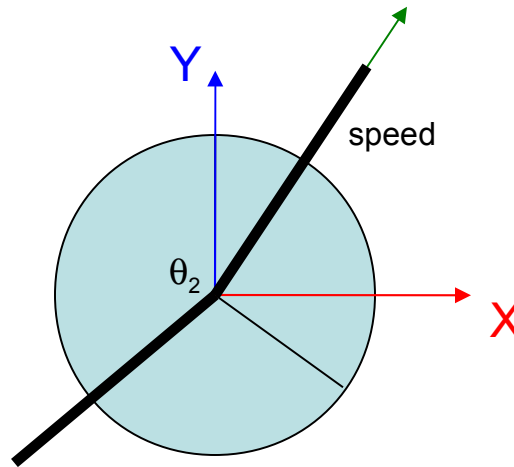
$$\sin(\theta_1) = \frac{M_1}{\text{speed}}$$

$$M_1 = \text{speed} \cdot \sin(\theta_1)$$

Sanity check:  $\sin(\theta = 0) = 0$ ,  $\sin(\theta = 90^\circ) = 1 = \text{full speed}$ ,  $\sin(\theta = -) = -$



# Wheel 2

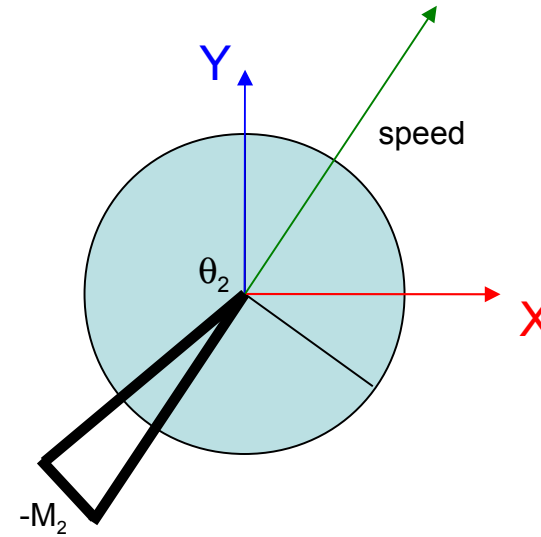
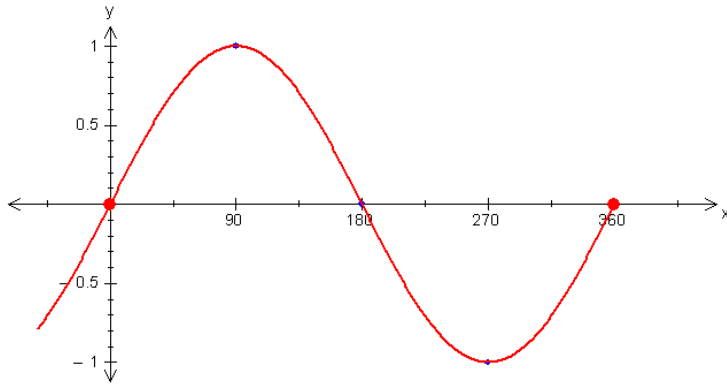


$$\theta_2 = \alpha_2 - \phi$$

$$M_2 = \text{speed} \cdot \sin(\theta_2)$$

Same equation!

# Wheel 2



$$\sin(\theta + 180) = -\sin(\theta)$$